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## SECURITY FLAWS IN AN IMPROVED TIMESTAMP-BASED REMOTE USER AUTHENTICATION SCHEME

JUAN QU

School of Mathematics and Statistics, Chongqing Three Gorges University, Wanzhou, Chongqing, 404000, China

Abstract. Recently, Awasthi et al. proposed a timestamp-based remote user authentication scheme. We point out that their scheme is vulnerable to smart card loss attack, offline password guessing attack and does not preserve anonymity of user. To overcome these flaws, we propose a new remote user authentication scheme. We also show that the proposed scheme not only solves the weaknesses which exist in Awasthi et al.'s scheme, but also can provide session key for the further communication.

**Keywords**: Authentication; Cryptanalysis; User anonymity; Stolen smart card attack; Offline password guessing attack.

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# 1. Introduction

With the repaid development of the Internet, the demand of Internet services is increasing. Remote user authentication is a mechanism which allows the user and the server to mutually authenticate the legitimacy of each other over public network. Since Lamport[1] proposed a password authentication protocol, ample of smart card based authentication protocols have been proposed[2]-[5]. In 1999, Yang and Shieh[6] proposed two password

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### JUAN QU

authentication schemes with smart cards. Later, Fan[7] proposed an enhancement scheme to improve the security of Yang and Shieh's password authentication scheme. In 2003, Wang et al.[8] showed that an intruder was able to construct a forged login request from the intercepted legitimate login requests. In the same year, Shen et al.[9] proposed a modified scheme of the Yang-Shieh's scheme to withstand the forged login attack and provide mutual authentication. But, Awasthi et al.[10] pointed out that Shen et al.'s scheme is still vulnerable to the forged login attack, and Awasthi et al. proposed an improvement scheme. However, we will show that Awasthi et al.'s scheme is vulnerable to smart card loss attack , offline password guessing attack and does not preserve anonymity of user. The remainder of this paper is organized as follows. In Section 2, we review a Prelimi-

naries. In section 3, Awasthi et al.'s scheme is shown. The security analysis is discussed in Section 4. In section 5, an enhanced authentication scheme using smart card and ECC is proposed. Finally, the conclusions are given in Section 6.

## 2. Preliminaries

In this section, we introduce the basic concepts of ECC. In all elliptic curve cryptosystem, the elliptic curve equation is defined as the form of  $E_p(a, b)$ :  $y^2 = x^3 + ax + b(\mod p)$ . Given an integer  $s \in F_p^*$  and a point  $P \in E_p(a, b)$ , the point-multiplication sP over  $E_p(a, b)$  can be defined as  $sP = P + P + P + \cdots + P(s \text{ times})$ . Generally, the security of ECC relies on the difficulties of the following problems.

Definition 1 Given two points P and Q over  $E_p(a, b)$ , the elliptic curve discrete logarithm problem (ECDLP) is to find an integer  $s \in F_p^*$  such that Q = sP.

Definition 2 Given three points P, sP, and tP over  $E_p(a, b)$  for  $s, t \in F_p^*$ , the computational Diffie-Hellman problem(CDLP) is to find the point (st)P over  $E_p(a, b)$ .

Definition 3 Given two points P and Q = sP + tP over  $F_p^*$  for  $s, t \in F_p^*$ , the elliptic curve factorization problem (ECFP) is to find two points sP and tP over  $E_p(a, b)$ .

### SECURITY FLAWS

## 3. Reviews of Awasthi et al.'s scheme

In 2011, Awasthi et al. analyzed the weaknesses of the Shen et al.'s scheme, and presented an improved remote authentication scheme. The modified scheme is composed for four phase: Initialization phase, Registration phase, Login phase and Authentication phase.

### 3.1.Initialization phase

Key information Center (KIC) is a trusted authority which generates global parameters. KIC also computes user's secret information and provides smart cards to users. KIC performs the following steps:

(1) Generates two large primes p and q and computes n = pq.

(2) Choose a prime number e and an integer d, such that  $e \cdot d \mod (p-1)(q-1) = 1$ , where e is the system's public key, and d is the corresponding private key, which should be provided to the server in a safe way.

(3) Find an integer g, which is a primitive element in both GF(p) and GF(q) and the public information of the system.

## 3.2. Registration phase

A new user  $U_i$  securely submits his identifier  $ID_i$  and password  $PW_i$  to the KIC. The KIC then performs the following steps:

(1)Genarate the smart card's identifier  $CID_i$  for the user  $U_i$  and  $h_i$  as  $CID_i = f(ID_i \oplus d)$ ,  $h_i = g^{PW_i \cdot d} \mod n$ , where f(x) is a one way function.

(2) Calculate the user's secret information  $S_i = CID_i^d \mod n$ .

(3) Write  $n, e, g, ID_i, S_i$  and  $h_i$  into smart card of  $U_i$  and issue the smart card to the user through a secure channel.

### 3.3.Login phase

User  $U_i$  performs the following steps:

(1) Choose a random number  $r_i$  and compute  $X_i$  and  $Y_i$  as follows:

 $X_i = g^{r_i \cdot PW_i} \mod n, \ Y_i = S_i \cdot h_i^{r_i \cdot f(ID_i, T_c)} \mod n$ , where  $T_c$  is the timestamp at the login device and f(x, y) is a one way function.

(2) User  $U_i$  sends  $M = (ID_i, X_i, Y_i, n, e, g, T_c)$  to the remote server S, where M is a login

request message of the user  $U_i$ .

## 3.4. Authentication phase

After receiving the login request message M from  $U_i$ , the remote server will perform the following steps to verify the correctness of M.

(1) Verify that  $ID_i$  is a valid user identifier. If it is not then reject the login request.

(2) Check the validity of  $T_c$ . If  $T_s - T_c > \Delta T$ , then the server rejects the login request, where  $T_s$  is the current timestamp at the remote server,  $\Delta T$  is expected legitimate time interval for transmission delay.

(3) Compute  $CID_i = f(ID_i \oplus d)$ .

(4) Check the equation  $Y_i^e = CID_i \cdot X_i^{f(ID_i,T_c)} \mod n$ . If it holds, accept the login request, otherwise reject.

(5)  $S \to M'$ :  $M' = (R, T'_s)$ , where  $R = (f(ID_i, T'_s))^d \mod n$  and  $T'_s$  is the current timestamp on the remote server. Upon receiving the message M' from the server, the user  $U_i$ verifies the server as follows.

(6) Check the time interval between  $T'_s$  and  $T'_c$ , where  $T'_c$  is the timestamp when the user  $U_i$  receives the message M'. If  $T'_c - T'_s > \Delta T$ , then  $U_i$  rejects the remote server, where  $\Delta T$  denotes the predetermined legitimate time interval of transmission delay.

(7) Compute  $R' = R^e \mod n$ . If  $R' \stackrel{?}{=} f(ID_i, T'_s)$ , accept the server otherwise reject server and disconnect it.

# 4. Flaws of Awasthi et al.'s scheme

In this section, we demonstrate that Awasthi et al.'s scheme is vulnerable to smart card loss attack , offline password guessing attack and does not preserve anonymity of user. The details of these flaws are described as follows.

## 4.1.Smart card loss attack

Smart card loss attack is that when the smart card is lost or stolen, unauthorized users can impersonate the user to login to the system or guess the password of the user using password guessing attack. If the user  $U_i$ 's smart card is lost or stolen, the attacker Acan extract the stored secret information  $(n, e, g, ID_i, S_i, h_i)$  stored in the smart card. Then, the attacker A can compute  $h_i^e = g^{PW_i \cdot d \cdot e} \mod n = g^{PW_i} \mod n$ . Then, the attacker A chooses a random number  $r'_i$  and computes  $X'_i = (h_i^e)^{r'_i} \mod n = g^{PW_i \cdot r'_i} \mod n$ ,  $Y'_i = S_i \cdot h_i^{r'_i \cdot f(ID_i, T'_c)} \mod n$ , where  $T'_c$  is the attacker A at the login device. In the following, the attacker A sends the login request message  $M' = (ID_i, X'_i, Y'_i, n, e, g, T'_c)$  to the remote server S. After receiving M', the remote server S verifies that the  $ID_i$  is a valid user identifier and check the validity of  $T'_s - T'_c \leq \Delta T$ . Then, the remote server S computes  $CID_i = f(ID_i \oplus d)$ , check the equation  $Y'_i = CID_i \cdot X'_i^{f(ID_i, T'_c)} \mod n$ . It is obvious that

$$Y_i'^e = S_i^e \cdot h_i^{r_i' \cdot f(ID_i, T_c') \cdot e} \mod n$$
  
=  $CID_i \cdot g^{PW_i \cdot d \cdot r_i' \cdot f(ID_i, T_c') \cdot e} \mod n$   
=  $CID_i \cdot g^{PW_i \cdot r_i' \cdot f(ID_i, T_c')} \mod n$   
=  $CID_i \cdot X_i'^{f(ID_i, T_c')} \mod n.$ 

Therefore, S accept the login request. According to the above analysis, when the user  $U_i$ 's smart card is stolen by the attacker A, then she/he can computes  $h_i^e$ . And with  $h_i^e$ , the attacker A can successful forge a valid login request message of the user  $U_i$ . Hence, Awasthi et al.'s scheme cannot resist the stolen smart card attack.

### 4.2.Offline password guessing attack

After the attacker A computes  $h_i^e = g^{PW_i} \mod n$  in the section 5.1. The attacker A can successfully guess the password of  $U_i$  as follows:

- (1) The attacker A randomly chooses  $PW_i^*$ ;
- (2) Computes  $g^{PW_i^*} \mod n$ ;
- (3) Verifies  $g^{PW_i} \mod n \stackrel{?}{=} g^{PW_i^*} \mod n$ .

### 4.3.User anonymity

User anonymity is an important feature that a practical authentication scheme should achieve. To prevent unauthorized entities from tracking the mobile user's movements. It is very important to ensure user anonymity such that user's real identity can only be recognized by server. In the login phase of Awasthi et al.'s scheme, user  $U_i$  sends the plaintext message  $M = (ID_i, X_i, Y_i, n, e, g, T_c)$  to the remote server S. The attacker can

### JUAN QU

easily get user's identity  $ID_i$  from the public channel. So, Awasthi et al.'s scheme fails in providing the privacy and anonymity of  $U_i$  during the login phase.

# 5. Proposed scheme

In this section, We propose our improved scheme that can protect against all the attacks mentioned in section 4. Suppose x is the secret key of KIC, and KIC computes  $Q = x \cdot P$ . Keeps secret x and publishes the public parameters P, n, Q,  $h(\cdot) : (0,1)^* \longrightarrow Z_n^*$ . Our scheme has four phases, registration, login, verification and password change phase. The details procedures are describes as follows.

### 5.1.Registration phase

1. user  $U_i$  chooses  $ID_i$ ,  $pw_i$  and computes  $pw_i \cdot P$ .

2.  $U_i$  submits his  $ID_i$  and  $pw_i \cdot P$  to KIC via a secret channel.

3. KIC computes  $h_i = x \cdot pw_i \cdot P$ ,  $S_i = h(x || ID_i) \cdot P$ ,  $T_i = h(ID_i || pw_i \cdot P)$ .

4. KIC issues smart card to  $U_i$  which contains values of  $S_i$ ,  $h_i$ ,  $T_i$ , and P via a secret channel.

## 5.2.Login phase

If  $U_i$  wants to access the server, he/she inserts smart card into the terminal, keys  $ID_i$ with  $pw_i$ , then the smart card verifies the equation  $h(ID_i||pw_i \cdot P) = T_i$  holds or not. If it holds, User  $U_i$  performs the following steps:

1. Chooses a random number  $r_i \in Z_n^*$  and computes  $R_i = r_i \cdot P$ ,  $X_i = r_i \cdot pw_i \cdot P$ ,  $Y_i = r_i \cdot h_i + h(S_i || r_i \cdot Q).$ 

2. User  $U_i$  sends  $M = (R_i, X_i, Y_i, P)$  to the remote server S, where M is a login request message of the user  $U_i$ .

### 5.3.Authentication phase

After receiving the login request message M from  $U_i$ , the remote server will perform the following steps to verify the correctness of M.

1. Computes  $S'_i = h(x || ID_i) \cdot P$ ,  $Y'_i = x \cdot X_i + h(S'_i || x \cdot R_i)$ ,  $U_i$  checks whether  $Y'_i \stackrel{?}{=} Y_i$ . If this holds, S authenticates  $U_i$  otherwise login request is rejected.

2. For mutual authentication, S selects a random number  $r_j \in Z_n^*$  and computes

 $R_j = r_j \cdot P, Z_i = h(r_j \cdot R_i || h(ID_i || R_i)),$  and then sends the mutual authentication message  $(R_j, Z_i)$  to  $U_i$ .

3. Upon receiving the mutual authentication message,  $U_i$  verifies  $Z'_i = h(r_i \cdot R_j || h(ID_i || R_i)) \stackrel{?}{=} Z_i$ . If this holds,  $U_i$  authenticates S otherwise login request is give up by  $U_i$ .

4. Now,  $U_i$  and S share the symmetric session key  $S_k = h(r_i \cdot r_j \cdot P || S_i)$  for performing further operations during a session.

### 5.4. Password-change phase

In the password-change phase, when a user wants to change his password  $pw_i$  with a new password  $pw_i^{new}$ , he inserts his smart card into smart card reader and enters his  $ID_i$  and password  $pw_i$ . The smart card performs the following operations without interacting with KIC:

1. Computes  $T_i^* = h(ID_i || pw_i \cdot P)$ . If  $T_i^* = T_i$ , then  $U_i$  is allowed to change the password, otherwise password-change phase is terminated.

2. Computes  $h_i^{new} = pw_i^{new} \cdot Q$  and replaces the old value of  $h_i$  with the new value. Now, the new password is successfully changed and this phase is terminated.

# 6. Cryptanalysis of the proposed scheme

In this section, we first describe the enhanced security features of our proposed scheme which is a modified form of Awasthi et al.'s scheme. Finally, the we summarize the functionality comparisons between our scheme and other remote user authentication schemes in Table 1. It is clear that our proposed scheme is more secure and reliable.

### 6.1. Resistance to smart card loss attack

Smart card attack cannot work on the improved scheme. When user  $U_i$ 's smart card is lost or stolen, though the attacker can extract the stored secret information  $(S_i, h_i, T_i, P)$ stored in the smart card, the attacker has no way to compute  $X_i$ ,  $Y_i$  to forge the login request message.

### 6.2. Resistance to offline-password guessing attack

The attacker has no way to carry out offline-guessing attack, because the password  $pw_i$ in  $h_i$ ,  $T_i$ , and  $X_i$  is protected by hash function and ECDLP problem.

### 6.3. user anonymity

In the proposed scheme, a user's real real identity is concealed in the  $Y_i$ , and each login request message is different. So, our proposed scheme preserve user anonymity.

### 6.4. Session key agreement

The user and the server establish a secure session key  $S_k = h(r_i \cdot r_j \cdot P || S_i)$  in each session. With this session key, the user and the remote server can exchange confidential data securely.

### 6.5.Performance comparison

	Shen et al.'s	Awasthi et	Proposed
	scheme	al.'s scheme	scheme
User anonymity	No	No	Yes
forged attack	Yes	Yes	No
Smart card loss attack	Yes	Yes	No
Mutual authentication	No	Yes	Yes
Key agreement	No	No	Yes

 Table 1. Comparison of security properties

Yes: Supported No: Not Supported

# 7. Summary

In this paper, we reviewed Awasthi et al.'s timestamp-based remote user authentication scheme. We found that Awasthi et al.'s scheme cannot defend against smart card loss attack, offline password guessing attack and does not preserve anonymity of a user. These flaws can cause the scheme to become unsecured. Finally, we propose an improvement scheme to overcome the identified problems and our scheme is more efficient and secure.

806

#### SECURITY FLAWS

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